A Quantitative Theory of Political Transitions*

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Abstract

We develop a quantitative theory of repeated political transitions driven by revolts and reforms. In the model, the beliefs of disenfranchised citizens play a key role in determining revolutionary pressure, which in interaction with preemptive reforms determine regime dynamics. We study the quantitative implications of the model by fitting it to data on the universe of political regimes existing between 1946 and 2010. The estimated model generates a process of political transitions that looks remarkably close to the data, replicating the empirical shape of transition hazards, the frequency of revolts relative to reforms, the distribution of newly established regime types after revolts and reforms, and the unconditional distribution over regime types.

Keywords: Democratic reforms, quantitative political economy, regime dynamics, revolts, transition hazards.

JEL Classification: D74, D78, P16.

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1 Introduction

This paper develops a quantitative theory of political transitions based on the evolution of beliefs regarding the regime’s strength. Traditionally, the literature has focused on explaining specific patterns of regime changes, focusing on isolated transition episodes.\(^1\) In this paper, we shift the focus to a macro perspective, aiming to account for a number of stylized facts in a unified framework.

Specifically, Section 2 of this paper documents five empirical regularities, which motivate the theoretical framework.

1. The evolution of political systems is shaped by both revolts and democratic reforms, with revolts being about three times as likely as reforms. Other modes of transition are secondary.

2. Transition hazards are declining in regime maturity. Newly established regimes are about three times as likely to be overthrown by a revolt and about six times as likely to implement a democratic reform compared to regimes older than 10 years.

3. Transition hazards are inverse “J-shaped” in the inclusiveness of political systems: Political systems at the extremes of the autocracy–democracy spectrum have smaller transition hazards than regimes near the center of the spectrum; full-scale democracies are overall most stable.

4. Revolts establish autocratic regimes; reforms establish democracies. Political systems near the center of the autocracy–democracy spectrum are unlikely to arise from either mode of transition.

5. The distribution of regime types is bi-modal, with mass concentrated towards the extremes of the autocracy–democracy spectrum.

This paper puts forward a theory of political transitions, which accounts for all five stylized facts above. In the model, the inclusiveness of a political system is defined by the enfranchised fraction of the population (“political insiders”). Transitions are governed by three main ingredients. First, reforms are rationalized by a preemptive logic as in Acemoglu and Robinson (2000b). Second, revolts are the outcome of a coordination game among the disenfranchised (“political outsiders”), introducing an intensive margin to revolting, defined by the degree of equilibrium coordination among outsiders. Finally, the degree of coordination is shaped

\(^1\)Exceptions include Acemoglu and Robinson (2001) and Besley and Persson (2018). The relation with these papers is discussed below.
by the beliefs of outsiders regarding the regime’s strength, which is privately observed by insiders at the beginning of each period.

The intensive margin of revolts in combination with learning implies that revolt hazards are decreasing in the regime’s strength as perceived by outsiders. This link between outsiders’ beliefs and revolt hazards is at the heart of our predictions. In particular, because in equilibrium concessions are associated with being weak, the link implies that small reforms will backfire and increase revolutionary pressure. Accordingly, when facing moderate threats, insiders rather take “tough stance” than preempting a subversive threat, explaining the prevalence of revolts documented in the data. Similarly, because transitions are more likely to occur when a regime is weak, outsiders rationally become more and more convinced that a regime is invulnerable as it matures, explaining the decline of transition hazards in regime maturity. The logic behind the inverse J-shape of transition hazards is a combination of two factors: On the one hand, full-scale democracies are intrinsically stable due to a lack of opposition (the extensive margin of revolting). On the other hand, similar to mature regimes, the most repressive autocracies are stable due to a low degree of coordination among outsiders (the intensive margin of revolting). This is because such regimes arise precisely when revolts are perceived as futile, making them less prone to future unrest as well. Finally, the two remaining regularities are again a consequence of small reforms backfiring and that revolts cannot grow too large as they would have been preempted otherwise.

The model is rich enough to lend itself to a quantitative exploration, mainly due to two modeling choices. First, transitions take place in a continuous polity space. This stands in contrast to the previous literature, which typically considers transitions between two or three exogenously defined political systems. Second, there are no exogenously absorbing states in our model, allowing us to compare model moments (computed at the stationary distribution) with their empirical counterparts. We demonstrate the quantitative potential by fitting the model to data on the universe of political regimes existing between 1946 and 2010. The model matches the data remarkably well. It is not only able to account for the above-listed regularities, but also quantitatively replicates the shape of transition hazards, conditional outcome distributions, and the stationary distribution of regime types.

We also use the estimated model to study circumstances under which successful democratization is likely. In the model, the belief or “sentiment” of outsiders is instrumental for creating a window of opportunity, in which democratization is possible. Only if outsiders perceive the regime as sufficiently vulnerable, they are likely to coordinate on large revolts and regimes are inclined to implement reforms to preempt them. However, due to the presence of asymmetric information, regimes generally do not find it optimal to completely preempt
a given threat of revolt. As a result, episodes in which democratization is possible are also marked by high revolt hazards, and the political system emerging from such “critical junctures” is determined by chance and random variations in the state of the world. Moreover, because newly established democracies emerge precisely when the regime is revealed to be most vulnerable, they are susceptible to counter-revolts by small but highly coordinated groups of outsiders. The model thus suggests that successful democratization critically hinges on the extent of the initial push for democratization. While reforms that enfranchise between 75% and 85% of the population have a cumulative failure rate of over 80 percent after 25 periods, the failure rate drops to 12 percent if reforms initially enfranchise more than 95% of the population.

To the best of our knowledge, this paper is first to develop a quantitative theory of political transitions. Our theory builds on several ingredients present in the existing literature. Specifically, the idea that reforms are means to credibly preempt a looming revolt has been standard in the literature since Acemoglu and Robinson (2000b), Conley and Temini (2001), and Boix (2003). Similarly, the view that revolts are the outcome of a coordination game has a long tradition in political science (e.g., Tullock, 1971; Granovetter, 1978; Kuran, 1989; Lohmann, 1994; Casper and Tyson, 2014). Finally, asymmetric information has been used to rationalize conflict along the equilibrium path in, e.g., Acemoglu and Robinson (2000a), Boix (2003), Hirshleifer, Boldrin and Levine (2009), Bueno de Mesquita (2010), and Ellis and Fender (2011).

Relative to existing works, a major advance of this paper is the development of a unified framework of repeated political transitions driven by both reforms and revolts. Closely related to our framework, Acemoglu and Robinson (2001) and Besley and Persson (2018) study models of repeated reforms and revolts. However, because transitions are exogenously restricted to alternate between two regimes of fixed size, these papers mechanically fix the revolt–reform ratio at unity in addition to fully predetermining transition outcomes, preventing a quantitative analysis along the lines of this paper.  

Another distinctive feature of our model is the continuity of the polity space, which is central to our predictions about the distribution of regime types. In that regard, our paper relates to the literature on voluntary suffrage extensions such as Bourguignon and Verdier (2000), Lizzeri and Persico (2004), and Llavador and Oxoby (2005). These papers also endogenize the scope of reforms, but abstract from revolts and regime dynamics, which

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2Besley and Persson (2018) consider two different modes of democratization. However, the relative frequency of democratization to regime reversals is similarly fixed at unity. Ticchi, Verdier and Vindigni (2013) consider an environment based on only coercive takeovers, in which regimes also alternate between autocracy and democracy.
are both key to our approach.\footnote{Our approach to endogenize the outcomes of political transitions also relates to a growing literature on dynamic voting games, which studies equilibrium coalitions in rich state spaces (Justman and Gradstein, 1999; Jack and Lagunoff, 2006; Gradstein, 2007; Acemoglu, Egorov and Sonin, 2008, 2012, 2015; Lagunoff, 2009; Bai and Lagunoff, 2011). However, given their focus on the composition of coalitions, these papers typically do not pin down a specific mode of transition between regimes, nor do they allow for forcible attempts to obtain power by means of revolt.}

The ability of our model to account for the data is also complementary to a number of empirical studies presenting direct evidence for the ingredients at the heart of our theory. Przeworski (2009), Aidt and Jensen (2014), and Aidt and Franck (2015) present evidence supporting the preemptive logic of reforms. Aidt, Leon and Satchell (2017), Enikolopov, Makarin and Petrova (2018), Manacorda and Tesei (2018), and Gonzalez (2019) present evidence supporting coordination as an essential element of revolts. Finally, Finkel, Gehlbach and Olsen (2015) document that halfhearted reforms may fuel revolts consistent with the idea that outsiders learn about regime strength.

The remainder of the paper is structured as follows. The next section presents a list of empirical regularities that are the target for our theoretical model. The model itself is developed in Section 3. In Section 4, we estimate the model and study its ability to account for the data. In Section 5, we describe the working of the model in detail and provide intuition for the forces explaining the data. In Section 6, we study the model’s implications for the formation and survival of democracies. In Section 7, we revisit the regularities motivating the model and discuss inasmuch they are consistent with alternative theories. Section 8 concludes.

2 Evidence on Political Transitions

This section presents a list of stylized facts about regime dynamics, which motivates the theoretical framework developed in the next sections.

The presented regularities are based on the universe of political regimes existing between 1946 and 2010, combining information from three datasets. First, we obtain the universe of regime spells from Geddes, Wright and Frantz (2014), who define regimes based on the identity of the ruling group. Second, we use the Polity IV Project’s polity index (Marshall, Gurr and Jaggers, 2017) to assign a regime type to each regime spell, which ranks political regimes on a 21-point scale between autocratic and democratic (normalized to values between 0 and 1). Finally, we treat any substantial change in the composition of regime insiders, as indicated by the turnover dates of regime spells, as transition events. Whenever available, we use the classification provided by Geddes, Wright and Frantz (2014) to classify transition events. Otherwise, we match transitions to leader changes collected by the Archigos Database.
Table 1: Frequency of Transition Events

<table>
<thead>
<tr>
<th>Transition event</th>
<th>Frequency</th>
<th>Share</th>
<th>Yearly hazard</th>
</tr>
</thead>
<tbody>
<tr>
<td>Revolt</td>
<td>188</td>
<td>0.56</td>
<td>0.0213</td>
</tr>
<tr>
<td>Democratic reform</td>
<td>66</td>
<td>0.20</td>
<td>0.0075</td>
</tr>
<tr>
<td>Autocratic consolidation</td>
<td>19</td>
<td>0.06</td>
<td>0.0021</td>
</tr>
<tr>
<td>Foreign imposition</td>
<td>16</td>
<td>0.05</td>
<td>0.0018</td>
</tr>
<tr>
<td>Other/unknown</td>
<td>49</td>
<td>0.14</td>
<td>0.0055</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>338</strong></td>
<td><strong>1.00</strong></td>
<td><strong>0.0382</strong></td>
</tr>
</tbody>
</table>

Notes.—The table reports number of occurrences for each transition type for all regime changes between 1946 and 2010, as well as frequencies normalized by total transitions (shares) and by country-years (yearly hazards).

of Political Leaders (Goemans, Gleditsch and Chiozza, 2009) and classify them according to the nature of the observed leader change. The resulting database covers 485 regime spells and 329 transitions in 155 countries. Online Appendix A.1 describes the construction of the dataset in detail.

**Fact 1:** The most frequent modes of transition are revolts and democratic reforms, with revolts being about three times as likely as reforms.

Our definition of revolts encompasses all forms of coercive takeovers by domestic actors (popular uprisings, power struggles between competing factions, and coups). Democratic reforms are peaceful transitions that lead to a more democratic political system. Together, revolts and reforms constitute 75 percent of all observed transition events. This corresponds to about .021 revolts and .008 reforms per country-year. The remaining transitions occur either via autocratic consolidations (peaceful transitions towards more autocratic polities, six percent), foreign imposition (five percent), or cannot be categorized based on the available information (14 percent). See Table 1 for further details.

**Fact 2:** Transition hazards are declining in regime maturity.

Figure 1 plots the transition hazards for our data.\(^5\) Newly established regimes are about...

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\(^4\)Geddes, Wright and Frantz (2014) define regime spells as uninterrupted reign of the same group of political elites. By their definition, coups constitute a transition only if they substantially alter the composition of the ruling group. In this regard, power struggles that, e.g., replace one military leader by another from the same group of military leadership do not constitute a transition.

\(^5\)The hazards are estimated by differencing and smoothing over Nelson-Aalen estimates for the cumulative hazard rate and are adjusted for left and right censoring. All findings are robust to controlling for the current political system and region fixed effects (see Online Appendix A.2 for details). Similar patterns have been documented by Sanhueza (1999) and Svolik (2008, 2015). Likewise, Bienen and van de Walle (1989, 1992) and Bueno de Mesquita et al. (2003) find a declining risk of loosing power at the level of political leaders.
Fact 3: Transition hazards are inverse “J-shaped” in the inclusiveness of political systems.

The regularity that regimes at the extremes of the political spectrum are most stable has been documented by a number of recent studies (e.g., Bremmer, 2006; Gates et al., 2006; Goldstone et al., 2010; Knutsen and Nygård, 2015). To investigate the pattern in our data, we estimate a Cox model with a cubic spline in the polity dimension (see Online Appendix A.2 for further details). Figure 2 plots the predicted relationship between polities and hazard ratios, normalized relative to the most autocratic regimes (with polity score equal to zero). Full-scaled democracies (with polity score of one) are least vulnerable to transitions with a relative hazard of approximately $1/5$. Hybrid regimes, in contrast, are on average up to four times as likely to undergo a transition compared to the most autocratic regimes.

Fact 4: Revolts establish autocratic regimes; reforms establish democratic regimes.

Figure 3 shows the conditional distribution over political systems arising from revolts and reforms. The median revolt establishes an (“autocratic”) regime with a polity score of 0.2. The median reform establishes a (“democratic”) regime with a polity score of 0.8. Political systems near the center of the autocracy–democracy spectrum are unlikely to arise from either mode of transition.6

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6See also Gleditsch and Choung (2004); Gleditsch and Ward (2006); Celestino and Gleditsch (2013); Derpanopoulos et al. (2016). The results are also consistent with a number of qualitative studies documenting...
Figure 2: Estimated hazard ratios of political systems. Notes.—Hazard ratios are estimated by a Cox regression with a cubic spline in the polity dimension. All hazard rates are for the combined failure due to reform and revolt, and are normalized relative to the combined hazard of regimes with a polity score of zero. Shaded bands correspond to 80 percent bootstrap confidence intervals, clustered at the country level.

Figure 3: Empirical distribution of political systems arising from revolts (left panel) and reforms (right panel). Notes.—Shaded bands correspond to 80 percent bootstrap confidence intervals, clustered at the country level.
Figure 4: Empirical distribution of political systems between 1946 and 2010. Notes.—Unit of observation are country-days. Shaded bands correspond to 80 percent bootstrap confidence intervals, clustered at the country level.

Fact 5: The distribution of regime types (polities) is bi-modal, with mass concentrated towards the extremes.

Finally, as illustrated in Figure 4, most mass of the empirical distribution over regime types is concentrated towards the extremes of the political spectrum: The combined mass of observations with a polity score \( \leq 0.25 \) and a polity score \( \geq 0.75 \) is 84 percent.

3 The Model

We set up a simple, dynamic model of repeated political transitions that are driven by revolts and reforms. Political systems are defined by the fraction of the population with access to power and can attain any value in \([0, 1]\).

3.1 Setup

We consider an infinite horizon economy, populated by overlapping generations of two-period lived agents. Each generation consists of a continuum of agents with mass equal to 1. At time \( t \), fraction \( \lambda_t \) of the population is represented by the franchise; the remaining agents are excluded from political power. We refer to these two groups as (political) “insiders” and “outsiders.”

When born, the distribution of political power among the young is inherited from their parent generation; that is, \( \lambda_t \) agents are born as insiders, while \( 1 - \lambda_t \) agents are born as

that democracies are unlikely to arise without a reform process (Rustow, 1970; O’Donnell and Schmitter, 1986; Karl, 1990; Huntington, 1991).
outsiders. Agents who are born as outsiders can attempt to overthrow the current regime and thereby acquire political power. To this end, outsiders choose individually and simultaneously whether or not to participate in a revolt. Because all political change will take effect at the beginning of the next period (see below), only young outsiders have an interest in participating in a revolt. We denote young outsider $i$’s choice by $\phi_{it} \in \{0, 1\}$ and use the aggregated mass of supporters, $s_t = \int \phi_{it} \, di$, to refer to the size of the resulting revolt.

Given the mass of supporters $s_t$, the probability that a revolt is successful is given by

$$p(\theta_t, s_t) = \theta_t h(s_t),$$

(1)

where $\theta_t \in [0, 1]$ is a random state of the world that reflects the vulnerability of the regime or its ability to withstand a revolt, and $h$ is an increasing and twice differentiable function, $h : [0, 1] \to [0, 1]$, with $h(0) = 0$. Intuitively, the threat of a revolt to the current regime is increasing in the mass of revolutionaries and in the regime’s vulnerability. When a revolt has no supporters ($s_t = 0$) or the regime is not vulnerable ($\theta_t = 0$), the regime survives with certainty.

The state of $\theta_t$ follows a (commonly known) Markov process with c.d.f. $G(\theta_t|\theta_{t-1})$ and is assumed to have full support on $[0, 1]$. At the beginning of each period, insiders learn the current realization of $\theta_t$. By contrast, outsiders do not observe $\theta_t$ directly and instead use Bayes’ law to form beliefs over its current realization based on the history of past political transitions. We use $F_t$ to denote the belief of outsiders over $\theta_t$ at the beginning of period $t$.

After learning the realization of $\theta_t$, insiders may try to alleviate the threat of a revolt by conducting reforms. We follow Acemoglu and Robinson (2000b) by modeling these reforms as an extension of the franchise to outsiders, which is effective in preventing them from supporting a revolt. Generalizing this mechanism to a continuous polity space, we allow insiders to continuously extend the regime by any fraction, $x_t - \lambda_t$, of young outsiders, where $x_t \in [\lambda_t, 1]$ denotes the reformed political system. Because preferences of insiders will be perfectly aligned, there is no need to specify the decision making process leading to $x_t$ in detail.

Given the (aggregated) policy choices $s_t$ and $x_t$, and conditional on the outcome of a revolt, the political system evolves as follows:

$$\lambda_{t+1} = \begin{cases} s_t & \text{if the regime is overthrown, and} \\ x_t & \text{otherwise.} \end{cases}$$

(2)

When a revolt fails, reforms take effect and the old regime stays in power. The resulting
political system in \( t + 1 \) is then given by \( x_t \). In the complementary case, when a revolt succeeds, those who have participated will form the new regime. Note that this specification prevents non-revoltting outsiders from reaping the benefits from overthrowing a regime so that there are no gains from free-riding in our model.

To complete the model description, we still have to specify how payoffs are distributed across the two groups of agents at \( t \). As for outsiders, we assume that they receive a per period payoff of \( \gamma_{it} \) that is privately assigned to each agent at birth and is drawn from a uniform distribution on \([0, 1]\). This heterogeneity is meant to reflect differences in the propensity to revolt, possibly resulting from different degrees of economical or ideological adaption to a regime. Outsiders’ payoffs remain constant over their life if they abstain from revolting, and otherwise change conditional on the success of the revolt (detailed below).

In contrast, insiders enjoy per period payoffs \( u(\lambda_t) \), where \( u \) is twice differentiable, \( u' < 0 \), and \( u(1) \) is normalized to unity. We think of \( u(\cdot) \) as a reduced form function that captures the various benefits of having political power (e.g., from extracting a common resource stock, implementing preferred policies, etc.).\(^7\) Note that \( u' < 0 \) implies that extending the regime is costly for insiders (e.g., because resources have to be shared, or preferences about policies become less aligned). Also, \( u(1) = 1 \) implies that \( u(\lambda_t) \geq \gamma_{it} \) for all \( \lambda_t \) and \( \gamma_{it} \); that is, being part of the regime is always desirable. In the case of full democracy (\( \lambda_t = 1 \)) all citizens are insiders and enjoy utility normalized to the one of a perfectly adapted outsider.

To simplify the analysis, we assume that members of an overthrown regime and participants in a failed revolt become worst-adapted to the new regime (\( \gamma_{it} = 0 \)).\(^8\) For the upcoming analysis it will be convenient to define the (future) utility of agents that are born at time \( t \), which is given by:

\[
V^I(\eta_t, x_t) = (1 - \eta_t)u(x_t),
\]

\[
V^O(\eta_t, \gamma_{it}, s_t, \phi_{it}) = \phi_{it}\eta_t u(s_t) + (1 - \phi_{it}) \gamma_{it}.
\]

Here \( \eta \in \{0, 1\} \) is an indicator evaluating to unity if the regime is overthrown, and superscripts \( I \) and \( O \) denote agents that are born as (or are newly enfranchised) insiders and outsiders, respectively. In both cases, the terms correspond to the second period payoffs accruing from

\(^7\)One could microfound \( u \) as a value function where all policy choices associated with having political power—except enfranchising political outsiders—are chosen optimally. Subsuming these decisions into \( u \) allows us to tractably explore the dynamics of political systems emerging from the interplay of reforms and revolts. All other policy choices still affect our analysis inasmuch as they determine the shape of \( u \).

\(^8\)In our dataset, 83 percent of overthrown leaders are killed, imprisoned or sentenced to exile under the new regime. Similar punishments are common for supporters of failed insurgencies, making the assumption that the losing party is worst-adapted arguably realistic. Further note that this assumption effectively maximizes the cost of engaging in political confrontation.
date \( t + 1 \) (which are a function of date-\( t \) choices). The first period payoffs are omitted, as they are unaffected by the policy choices of generation \( t \).

The timing of events within one period can be summarized as follows:

1. The current state of \( \theta_t \) realizes and is revealed to insiders.

2. Insiders may extend political power to a fraction \( x_t \in [\lambda_t, 1] \) of the population.

3. Outsiders, if excluded from the reform, individually and simultaneously decide whether or not to participate in a revolt.

4. Transitions according to (1) and (2) take place, period \( t + 1 \) starts with the birth of a new generation, and payoffs are realized.

Two remarks The core of our model defines an interaction between revolutionary pressure and preemptive reforms in the tradition of Acemoglu and Robinson (2000b), Conley and Temini (2001), and Boix (2003). Implicit in the preemptive logic of reforms is the requirement that extending the franchise entails a credible commitment to share political power that is not easily reversible. Accordingly, our notion of inclusiveness, \( \lambda_t \), is best understood as the fraction of citizens that are protected from losing political power, either because of hard-to-overturn institutional guarantees as in Acemoglu and Robinson (2000b), or because each insider is indispensable for the stability of the ruling coalition as in Acemoglu, Egorov and Sonin (2012). In line with this interpretation of \( \lambda_t \), as well as with the low frequency of autocratic consolidations in the data, our model abstracts from the possibility of “adverse reforms”.\(^9\)

Relatedly, we assume that reforms are effective in the sense that newly enfranchised outsiders (as well as agents born as insiders) do not rebel against the regime. As formally proved in Online Appendix B.1, this is indeed internally consistent within our setting, as newly enfranchised outsiders (and born insiders) would never support a revolt if given the choice.

Equilibrium definition We characterize the set of perfect Bayesian equilibria subject to two equilibrium refinements. First, we rule out “instable” coordination among outsiders on \( s_t = 0 \), whenever an infinitesimal small chance of success would persuade a non-marginal

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\(^9\)In addition to the aforementioned reasons, abstracting from adverse reforms is also analytically convenient, as it allows us to treat insiders as a homogeneous group, rather than providing an explicit model of within-regime power struggles that may result in the ejection of certain subgroups.
mass of outsiders to revolt.\textsuperscript{10} Second, we limit attention to equilibria that are consistent with the D1 criterion introduced by Cho and Kreps (1987), a standard refinement for signaling games.\textsuperscript{11} As detailed below (see Footnote 14), the refinement improves the predictive power of our model by selecting a unique equilibrium, but is inconsequential for our main predictions.

Before defining equilibrium, it is useful to fix some notation. First, as already noted, we use $F_t$ to denote the “prior” belief of young outsiders born at date $t$, which is formed using Bayes’ law (if applicable) given all publicly observable information available at the beginning of period $t$. Specifically, we have

$$F_t(\vartheta) = \Pr[\theta \leq \vartheta | \delta_{t-1}]$$

for any publicly observable history $\delta_t \equiv \{(\phi_{i\tau}, x_{\tau}, \lambda_{\tau}, \eta_{\tau})\}_{\tau=0}^t$ that is reached along the equilibrium path with strictly positive probability. As usual, off-equilibrium beliefs can be chosen freely, subject to the restrictions imposed by the D1 criterion. Similarly, we use $\hat{F}_t$ to denote the interim belief of outsiders, which combines $F_t$ with the information signaled by reforms $x_t$:

$$\hat{F}_t(\vartheta) = \Pr[\theta \leq \vartheta | \delta_{t-1}, x_t]$$

for all $(\delta_{t-1}, x_t)$ reached along the equilibrium path. Here we do not index $F_t$ and $\hat{F}_t$ by $i$, since they will be pinned down uniquely by the D1-refinement—even off the equilibrium path—ruling out any scope for belief heterogeneity across outsiders.

We are now ready to define the equilibrium for our model. To simplify notation, we only define pure strategies here, since only pure strategy equilibria exist in our game (see the proofs to Propositions 1 and 2).

**Definition.** Given a history $\bar{\delta} = \{\delta_r, \theta_r\}_{r=0}^{t-1}$, an equilibrium in this economy consists of strategies $x_{\bar{\delta}} : \theta \mapsto x$ and $\{\phi_{i\bar{\delta}} : (\hat{F}, x) \mapsto \phi_i\}$, and (interim) beliefs $\hat{F}_{\bar{\delta}} : x \mapsto \hat{F}$, such that for all histories $\bar{\delta}$:

a. Reforms $x_{\bar{\delta}}$ maximize insider’s expected utility $V^I(p_{\bar{\delta}}, x_{\bar{\delta}})$ given outsiders’ beliefs $\hat{F}_{\bar{\delta}}$ and strategies $\{\phi_{i\bar{\delta}}\}$;

\textsuperscript{10}In a previous version of this paper (Buchheim and Ulbricht, 2014), we demonstrate that this restriction is formally equivalent to characterizing the set of trembling-hand perfect equilibria (at the expense of additional notation). An alternative (and outcome-equivalent) approach to rule out these instabilities would be to restrict attention to equilibria which are the limit to a sequence of economies with a finite number of outsiders, where each agent’s decision has non-zero weight on $s_t$.

\textsuperscript{11}The D1 criterion restricts outsiders to believe that whenever they observe a reform $x'$ that is not conducted in equilibrium, the reform has been implemented by a regime with vulnerability $\theta'$, for which a deviation to $x'$ would be most attractive in the sense that it is beneficial under the largest set of possible inferences $\{\theta\}$ about the regime’s vulnerability.
b. Each outsider’s revolt choice $\phi_{i\delta}$ maximizes $\mathbb{E}_{\hat{F}_\delta}\left\{V^O(p_{\delta}, \gamma_{i\delta}, s_{\delta}, \phi_{i\delta})\right\}$ given insiders’ reforms $x_{\delta}$, other outsiders’ revolt choices $\{\phi_{j\delta}\}_{j \neq i}$, and beliefs $\hat{F}_\delta$.\(^{12}\)

c. Beliefs $\hat{F}_\delta$ are obtained using (6) for all $(\delta_{t-1}, x_t)$ along the equilibrium path, and satisfy the D1 criterion otherwise;

d. The evolution of $(\lambda_t, \eta_t)$, contained in $\bar{\delta}$, is consistent with (1) and (2);

e. Coordination among outsiders is stable; i.e., perturbing perceived coordination $\hat{s}_{\delta}$ by $\epsilon$ changes the coordination outcome $s_{\bar{\delta}}$ by at most $\nu$ where $\nu \to 0$ as $\epsilon \to 0$.

3.2 Equilibrium Characterization

As a result of the overlapping generations structure of the model, the characterization of equilibrium can be separated into a sequence of “generation games” between young insiders and young outsiders. Generations are linked across periods through the evolution of the payoff-relevant state, given by $S_t \equiv (\theta_t, \lambda_t, F_t)$.

The generation game at $t$ consists of two stages. In the second stage, outsiders have to choose whether or not to support a revolt. Because the likelihood that a revolt succeeds depends on the total mass of its supporters, outsiders face a coordination problem in their decision to revolt. In the first stage, prior to this coordination problem, insiders decide on the degree to which political power is extended to outsiders. On the one hand this will decrease revolutionary pressure along the extensive margin by contracting the pool of potential insurgents. On the other hand, extending the regime may also contain information about the regime’s vulnerability. As a result, reforms may increase revolutionary pressure along the intensive margin by increasing coordination among outsiders who are not subject to reforms. Insiders’ policy choices will therefore be governed by signaling considerations.

We proceed by backward induction in solving for the equilibrium of the generation game, beginning with the outsiders’ coordination problem.

Stage 2: Coordination among outsiders  Let $\hat{\theta}_t \equiv \mathbb{E}_{\hat{F}_t}\{\theta_t\}$ define the interim-expectation of outsiders regarding $\theta_t$. Because $\mathbb{E}_{\hat{F}}\{V^O(\cdot)\}$ is linear in $\theta$, $\hat{\theta}_t$ is a sufficient statistic for $\hat{F}_t$. For any belief, $(\hat{\theta}_t, \hat{s}_t) \in [0, 1]^2$, individual rationality requires all outsiders to choose $\phi_{i\delta}$ so as to maximize their expected utility $\mathbb{E}_{\hat{F}}\{V^O(\cdot)\}$. Specifically, an outsider with opportunity cost

\(^{12}\)Throughout we use subscripts to $\mathbb{E}$ to indicate the probability measure with respect to which the expectation is taken.
γ_{it} \text{ will participate in a revolt if and only if }
\begin{equation}
\gamma_{it} \leq p(\hat{\theta}_t, \hat{s}_t) u(\hat{s}_t) \equiv \bar{\gamma}(\hat{\theta}_t, \hat{s}_t). \tag{7}
\end{equation}

Here, \(\bar{\gamma}(\hat{\theta}_t, \hat{s}_t)\) is the expected benefit of supporting a revolt of size \(\hat{s}_t\). Since \(\bar{\gamma}\) is independent of \(\gamma_{it}\), it follows that in any equilibrium the set of outsiders who support a revolt at \(t\) is given by the agents who are least adapted to the current regime. For any \(\bar{\gamma}\), the size of the resulting revolt is then given by
\begin{equation}
s_t = (1 - x_t) \min\{\bar{\gamma}(\hat{\theta}_t, \hat{s}_t), 1\}. \tag{8}
\end{equation}

In equilibrium, it must hold that \(s_t = \hat{s}_t\). Accordingly, the share of outsiders supporting a revolt is pinned down by the fixed point to (8). To guarantee that a well-behaved fixed point exists, we impose the following assumption.

**Assumption 1.** Let \(\psi(s) \equiv h(s) \cdot u(s)\). Then, \(\psi' \geq 0, \psi'' \leq 0\) and \(\lim_{s \to 0} \psi'(s) = \infty\).

Assumption 1 imposes that the participation choices of outsiders are strategic complements. This requires that the positive effect of an additional supporter on the success probability outweighs the negative effect of being in a slightly larger regime after a successful revolt. To ensure existence, we further require that the positive effect of an additional supporter is sufficiently strong when a revolt is smallest, and is nonincreasing as revolts grow larger.

Equipped with Assumption 1, we obtain the following proposition.

**Proposition 1.** In any equilibrium, the mass of outsiders supporting a revolt at time \(t\) is uniquely characterized by the solution to (8), given by a time-invariant mapping \(s : (\hat{\theta}_t, x_t) \mapsto s_t\). The solution satisfies \(s(0, \cdot) = s(\cdot, 1) = 0\), increases in \(\hat{\theta}_t\), and decreases in \(x_t\).

All proofs are in the online appendix. Proposition 1 establishes the tradeoff of conducting reforms: On the one hand, reforms reduce support for a revolt along the extensive margin. In particular, in the limit where regimes reform to a full-scaled democracy, any threat of revolt is completely dissolved. On the other hand, if reforms signal that a regime is vulnerable, they may backfire by increasing support along the intensive margin.

**Stage 1: Reforms by insiders** We now turn to the insiders’ decision problem. Since more vulnerable regimes have higher incentives to reform than less vulnerable ones, conducting reforms will be associated with being intrinsically weak and, therefore, indeed increases coordination along the intensive margin. For the benefits along the extensive margin to justify these costs, reforms have to be far-reaching, inducing regimes to enfranchise a large
portion of the population whenever they conduct reforms. The next proposition describes the equilibrium schedule of reforms.

**Proposition 2.** Define insiders’ expected utility as $\tilde{V}^I(\theta, \hat{\theta}, x) \equiv V^I(\theta h(s(\hat{\theta}, x)), x)$, and let $\xi$ be the differential equation solving\(^{13}\)

$$\xi'(\theta) = -\tilde{V}^I_2(\theta, \theta, \xi)/\tilde{V}^I_3(\theta, \theta, \xi) > 0$$

with boundary condition $\xi(1) = \arg\max_{\xi \in [0,1]} \tilde{V}^I(1, 1, \xi)$. Then, in any equilibrium, policy choices of insiders are uniquely defined by the time-invariant function, $x : (\theta_t, \lambda_t, F_t) \mapsto x_t$,

$$x(\theta, \lambda, F) = \begin{cases} \lambda & \text{if } \theta \leq \bar{\theta}(\lambda, F) \\ \xi(\theta) & \text{if } \theta > \bar{\theta}(\lambda, F) \end{cases}$$

with $\xi(\theta) > \lambda$ for all $\theta > \bar{\theta}(\lambda, F)$. The threshold type, $\bar{\theta} : (\lambda_t, F_t) \mapsto \bar{\theta}_t$, is implicitly defined by (whenever a solution exists)

$$\tilde{V}^I(\bar{\theta}, \bar{\theta}, \xi(\bar{\theta})) = \tilde{V}^I(\bar{\theta}(\lambda, \lambda, F), \lambda), \tag{9}$$

and is otherwise given by $\bar{\theta} = 1$. Outsiders’ interim beliefs are defined by\(^{14}\), $\hat{\theta} : (\lambda_t, x_t, F_t) \mapsto \hat{\theta}_t$, with

$$\hat{\theta}(\lambda, x, F) = \begin{cases} \mathbb{E}_F\{\theta | \theta \leq \bar{\theta}(\lambda, F)\} & \text{if } x = \lambda \\ \xi^{-1}(x) & \text{if } \xi(\bar{\theta}(\lambda)) \leq x \leq \xi(1). \end{cases}$$

Proposition 2 describes equilibrium reforms as a function of $(\theta_t, \lambda_t, F_t)$. Because the logic behind these choices is the same for all values of $\lambda_t$ and $F_t$, we can discuss the underlying intuition keeping $(\lambda_t, F_t)$ fixed. To this end, Figure 5 plots reform choices (left panel) and the implied probability to be overthrown (right panel), fixing $\lambda_t = 0.1$ and $F_t(\theta) = \theta$. Extended versions of the figure with alternative values for $\lambda_t$ and $F_t$ can be found in Online Appendix E.

Whenever $\theta_t \leq \bar{\theta}(\lambda_t, F_t)$, insiders do not reform $(x_t = \lambda_t)$, implying a substantial threat for regimes with $\theta_t$ close to $\bar{\theta}_t$. To see the logic behind this, first consider Figure 6. Here we plot equilibrium beliefs (left panel) and the corresponding mass of insurgents (right panel) as functions of $x_t$. If there are no reforms, outsiders only know the average vulnerability,

\(^{13}\)Throughout, we use $f_i$ to denote the derivative with respect to the $i$-th argument of some function $f$.

\(^{14}\)Off the equilibrium path, beliefs are uniquely pinned down by the D1 criterion as $\hat{\theta}_t = \hat{\theta}(\lambda_t)$ for $x \in (\lambda_t, \xi(\bar{\theta}_t))$ and $\hat{\theta}_t = 1$ for $x > \xi(1)$, contributing to the overall uniqueness of the reform schedule. However, even without D1, reforms are always increasing, starting from a strictly positive pool at $x_t = \lambda_t$ and have a discontinuity at the marginally reforming regime $\bar{\theta}_t$. Accordingly, the D1 refinement merely pins down the precise shape of $\xi$, but is not substantial for generating any of the main features of the reform schedule.
\( \hat{\theta}_t^{\text{pool}} \equiv \mathbb{E}_{F_t}\{\theta_t|\theta_t \leq \bar{\theta}_t\} \), of all regimes pooling on \( x_t = \lambda_t \). By contrast, every extension \( x - \lambda_t > 0 \) of the regime leads to a non-marginal change in outsiders’ beliefs from \( \hat{\theta}_t^{\text{pool}} \) to \( \xi^{-1}(x) \geq \hat{\theta}_t \) and, therefore, causes a non-marginal increase in revolutionary pressure along the intensive margin. It follows that small reforms will backfire and *increase* the mass of insurgents as the increase in coordination dominates any marginal reduction in the group of potential insurgents along the extensive margin.

Furthermore, optimality of reforms requires that the benefit of reducing pressure compensates for insiders’ disliking of sharing power. Hence there exists a nonempty interval, depicted by \( [\bar{x}, \xi(\hat{\theta}_t)] \) in the right panel of Figure 6, in which reforms are effective, yet insiders prefer to “gamble for their survival” in order to hold on to the benefits of not sharing power. This causes a substantial threat for regimes with \( \theta_t \) close to \( \bar{\theta}_t \), which can reconcile a frequent

**Figure 5:** Equilibrium reforms and implied probability to be overthrown.

**Figure 6:** Equilibrium beliefs and implied mass of insurgents.
occurrence of revolts with the co-occurrence of preemptive reforms.\footnote{More precisely, gambling for survival increases the revolt hazard in two ways. Firstly, since at the margin more vulnerable regimes join the pool at \( x_t = \lambda_t \), these regimes obviously face a high threat by not reforming. Secondly, since these regimes also deteriorate the average pooling belief towards being more vulnerable, there is a further infra-marginal increase in the threat that affects all regimes without reforms.}

**Learning dynamics** Propositions 1 and 2 fully characterize actions at \( t \) conditional on the state \( S_t \). To complete the characterization of equilibrium, we have to describe how \( S_t \) evolves over time. The evolution of \( \theta_t \) and \( \lambda_t \) is described by the processes \( G \) and \( (2) \), leaving us to characterize the law of motion for \( F_t \).

Let \( \tilde{F}_t \) define the “posterior” belief of outsiders living at date \( t \), formed using Bayes’ law, given all publicly available information at the end of period \( t \),

\[
\tilde{F}_t(\vartheta) = \Pr[\theta \leq \vartheta|\delta_t].
\]

Intuitively, \( \tilde{F}_t \) combines the prior \( F_t \) with the information signaled by \( x_t \) (yielding the interim-belief \( \tilde{F}_t \)) and the information contained in whether or not the regime is overthrown, \( \eta_t \).

Once we have compute \( \tilde{F}_t \), we can use it to obtain the prior of the next generation, \( F_{t+1} \), by simply “forecasting” \( \theta_{t+1} \) using the law of motion for \( \theta_t \):

\[
F_{t+1}(\vartheta) = \int_0^\vartheta \int_0^1 G'(|\theta|\theta) \, d\tilde{F}_t(\theta) \, d\theta'
\]

We complete our equilibrium characterization with an explicit characterization of \( \tilde{F}_t \).

**Proposition 3.** Let \( M_i^t(\vartheta) \equiv \mathbb{E}_{F_t}\{\theta^i|\theta \leq \vartheta\} \) define the \( i \)-th (raw) moment of \( F_t(\theta|\theta \leq \vartheta) \). Then, along the equilibrium path, outsiders’ posterior is given by:

(i) if there is a reform attempt \( (x_t > \lambda_t) \),

\[
\tilde{F}_t(\vartheta) = \begin{cases} 
0 & \text{if } \vartheta < \theta_t \\
1 & \text{else,}
\end{cases}
\]

(ii) if there is a revolt and no reform attempt \( (x_t = \lambda_t \text{ and } \eta_t = 1) \),

\[
\tilde{F}_t(\vartheta) = \begin{cases} 
\frac{F_t(\theta) M_1^t(\theta)}{F_t(\theta_t) M_1^t(\theta_t)} & \text{if } \vartheta < \bar{\theta}_t \\
1 & \text{else,}
\end{cases}
\]
(iii) if there is no transition \((x_t = \lambda_t \text{ and } \eta_t = 0)\),

\[
\tilde{F}_t(\vartheta) = \begin{cases} 
F_t(\vartheta) & \text{if } \vartheta < \bar{\theta}_t \\
F_t(\bar{\theta}_t) \cdot \frac{1-h(s_t)M^1_t(\vartheta)}{1-h(s_t)M^1_t(\bar{\theta}_t)} & \text{if } \vartheta = \bar{\theta}_t \\
1 & \text{else.}
\end{cases}
\]

For later reference, it is useful to also compute the first two moments of \(\tilde{F}_t\). Specifically, using Proposition 3, the posterior mean and variance are given by

\[
\tilde{\mu}_t = \begin{cases} 
\theta_t & \text{if } x_t > \lambda_t \\
\frac{M^2_t(\bar{\theta}_t)}{M^1_t(\bar{\theta}_t)} & \text{if } x_t = \lambda_t \text{ and } \eta_t = 1 \\
\frac{M^1_t(\bar{\theta}_t) - h(s_t)M^2_t(\bar{\theta}_t)}{1-h(s_t)M^1_t(\bar{\theta}_t)} & \text{if } x_t = \lambda_t \text{ and } \eta_t = 0
\end{cases}
\]

and

\[
\tilde{\sigma}^2_t = \begin{cases} 
0 & \text{if } x_t > \lambda_t \\
\frac{M^2_t(\bar{\theta}_t) - \tilde{\mu}^2_t}{1-h(s_t)M^1_t(\bar{\theta}_t)} - \tilde{\mu}^2_t & \text{if } x_t = \lambda_t \text{ and } \eta_t = 1 \\
\frac{M^1_t(\bar{\theta}_t) - h(s_t)M^2_t(\bar{\theta}_t)}{1-h(s_t)M^1_t(\bar{\theta}_t)} & \text{if } x_t = \lambda_t \text{ and } \eta_t = 0.
\end{cases}
\]

Existence and uniqueness of equilibrium Proposotions 1–2 uniquely pin down insiders’ and outsiders’ actions conditional on the state \(S_t\), whereas Proposition 3 (in conjunction with \(G\) and (2)) pins down a unique law of motion for \(S_t\). We conclude that there is no scope for multiple equilibria in our model. Verifying that an equilibrium exists, then permits us to reach the following conclusion.

**Proposition 4.** There exists an equilibrium, in which for all histories \(\bar{\delta}\), policy mappings \(x_{\bar{\delta}}\) and \(\{\phi_{i\delta}\}_{i[0,1]}\), as well as beliefs \(F_{\delta}\) correspond to the time-invariant mappings underlying Propositions 1–3. Furthermore, for any given initial state \(S_0\), the equilibrium is unique.

### 4 Quantitative Implications for Regime Dynamics

To explore the empirical performance of the model, we fit it to a few key moments of the data. We first study the implications for the frequency of transitions, hazard rates, transition outcomes, and the stationary distribution of political systems. Overall, the model fits the patterns documented in Section 2 quite well, even those that are not targeted by the calibration. Then, in the next section, we provide intuition for our results and illustrate how the different features of the model contribute to matching the data.
4.1 Parametrization

We choose the following parametrization of the model. The utility of insiders and the likelihood of a successful revolt are given by \( u(\lambda) = 1 + \alpha_u(1 - \lambda) \) and \( h(s) = s^{\alpha_h} \). Here, \( \alpha_u \) is the marginal disutility of extending the regime, whereas \( \alpha_h \) defines the elasticity of \( p_t \) with respect to an additional revolutionary. The restrictions we imposed on \( u \) and \( h \) require \( \alpha_u, \alpha_h \in (0, 1) \) and \( \alpha_u \leq \alpha_h \). Based on some initial exploration, we found that the latter constraint is typically binding when trying to implement a stationary distribution with non-trivial mass on autocracies.\(^{16}\) Accordingly, we fix \( \alpha_u = \alpha_h \equiv \alpha \) to reduce the computational complexity of the estimation.

Next, we set \( G \) so that \( \theta_t \) follows a truncated AR(1) process,

\[
\theta_t = \min(\max(\rho \theta_{t-1} + \epsilon_t, 0), 1),
\]

with persistence rate \( \rho \in [0, 1) \) and innovations \( \epsilon_t \) that are i.i.d. normal with mean \( \mu_\epsilon \) and variance \( \sigma_\epsilon^2 \). Observe that for \( \sigma_\epsilon \) sufficiently small, the mean and variance of \( F_{t+1} \) are approximately given by:

\[
\begin{align*}
\mu_{t+1} &= \rho \bar{\mu}_t + \mu_\epsilon \\
\sigma_{t+1}^2 &= \rho^2 \sigma_t^2 + \sigma_\epsilon^2.
\end{align*} \tag{13} \tag{14}
\]

One challenge in simulating the model over long periods of time is that \( F_t \) typically does not stay within a given parametric family of distributions, making it difficult to keep track of beliefs over time. To address this issue, we approximate \( F_{t+1} \), derived in (10), by a Beta distribution with mean \( \mu_{t+1} \) and variance \( \sigma_{t+1}^2 \) matching the corresponding moments of \( F_{t+1} \) as given by (13) and (14). We explore the accurateness of the approximation in Online Appendix D, finding it to be extremely precise. Since the Beta distribution is fully parametrized by its first two moments, this approach allows us to efficiently keep track of outsiders’ beliefs using just \( \mu_t \) and \( \sigma_t^2 \).

With our approximation for \( F_t \), the state space reduces to \( \mathcal{S}_t = (\theta_t, \lambda_t, \mu_t, \sigma_t^2) \). Throughout our exploration, we will take the stand that \( \theta_t \) is unobserved by the statistician (as it is in the data), meaning that we will only look at moments where \( \theta_t \) is marginalized out. In addition to ensuring consistency with the empirical moments, this view turns out to be also convenient, as it allows us to eliminate \( \theta_t \) from \( \mathcal{S}_t \) when characterizing the stationary distribution, requiring

\(^{16}\)For small \( \alpha_u \), autocracies are less profitable and regimes tend to reform frequently, resulting in a large mass of democracies relative to autocracies.
The target moments are chosen to reflect the regularities presented in Section 2: (i) the unconditional mean and variance of roughly \( \hat{\alpha}, \hat{\rho}, \hat{\mu}, \hat{\sigma}_\epsilon \). The estimated parameter values are \( \hat{\omega} \) where \( \omega \equiv (\alpha, \rho, \mu, \sigma_\epsilon) \). We choose \( \omega \) to match, as closely as possible, nine empirical moments \( \hat{M} \) listed in Table 2 (further described below). Let \( M(\omega) \) denote the mapping from \( \omega \) to the corresponding model moments. A detailed description of the algorithm implementing \( M \) is given in Online Appendix C. Our estimator for \( \omega \) is given by

\[
\hat{\omega} = \arg\min_\omega \left( \hat{M} - M(\omega) \right)^\prime \hat{V}^{-1} \left( \hat{M} - M(\omega) \right),
\]

where \( \hat{V} \) is a diagonal matrix with the bootstrapped variances of \( \hat{M} \) along the diagonal. The estimated parameter values are \( \hat{\alpha} = .569, \hat{\rho} = .736, \hat{\sigma}_\epsilon^2 / (1 - \hat{\rho}^2) = .030 \), and \( \hat{\rho} = .9997 \). These values imply that elites in an autocratic system enjoy roughly 60 percent higher value than citizen in a full-scale democracy. The process for \( \theta \) is highly persistent, with unconditional mean and variance of roughly .736 and .030.

### 4.2 Calibration

The parameterized model is described by four parameters, \( \omega \equiv (\alpha, \rho, \mu, \sigma_\epsilon) \). We choose \( \omega \) to match, as closely as possible, nine empirical moments \( \hat{M} \) listed in Table 2 (further described below). Let \( M(\omega) \) denote the mapping from \( \omega \) to the corresponding model moments. A detailed description of the algorithm implementing \( M \) is given in Online Appendix C. Our estimator for \( \omega \) is given by

\[
\hat{\omega} = \arg\min_\omega \left( \hat{M} - M(\omega) \right)^\prime \hat{V}^{-1} \left( \hat{M} - M(\omega) \right),
\]

where \( \hat{V} \) is a diagonal matrix with the bootstrapped variances of \( \hat{M} \) along the diagonal. The estimated parameter values are \( \hat{\alpha} = .569, \hat{\rho} = .736, \hat{\sigma}_\epsilon^2 / (1 - \hat{\rho}^2) = .030 \), and \( \hat{\rho} = .9997 \). These values imply that elites in an autocratic system enjoy roughly 60 percent higher value than citizen in a full-scale democracy. The process for \( \theta \) is highly persistent, with unconditional mean and variance of roughly .736 and .030.

**Targeted moments** The empirical and simulated moments, targeted in our calibration, are presented in Table 2. All model moments are computed at the stationary distribution. The target moments are chosen to reflect the regularities presented in Section 2: (i) the

\[^{17}\text{In particular, exploiting that the information set of the statistician is aligned with the one of outsiders, we use a hidden state forward algorithm where instead of keeping track of} \theta_t \text{, we use} F_t \text{to keep track of distributions over} \theta_t \text{that are consistent with a particular (publicly observed) history} \delta = \{\lambda_{t+1}, \mu_{t+1}, \sigma_{\epsilon, t+1}\}_{t=0}^T.\]

\[^{18}\text{Specifically, we chose thresholds} \{.025, .075, ..., .975\}, \text{defining the edges between two adjacent grid points} \{\lambda_t, \lambda_{t+1}\}, \text{such that the mid-points of each} \lambda\text{-bin,} \{.05, .1, ..., .95\}, \text{match the desired discretization of} \lambda \text{in the interior of the grid. At the boundaries, we obtain} \lambda_1 = .0125 \text{and} \lambda_{N_{\lambda}} = .9875 \text{as the mid-points of the two most extreme} \lambda\text{-bins.}

\[^{19}\text{Observe that the standard deviation of the Beta distribution is bounded above by 1/2. We chose a log-linearly spaced grid for} \sigma_\epsilon \text{as the distribution over} \sigma_\epsilon \text{is strongly right-skewed.}

\[^{20}\text{The corresponding values for} \mu_e \text{and} \sigma_\epsilon \text{are} .197 \times 10^{-3} \text{and} .0040.\]
Table 2: Data Moments and Model Simulated Moments

<table>
<thead>
<tr>
<th>Fitted Moments</th>
<th>Data</th>
<th>Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Revolt–reform ratio</td>
<td>2.85</td>
<td>2.82</td>
</tr>
<tr>
<td></td>
<td>(0.39)</td>
<td></td>
</tr>
<tr>
<td>Revolt-hazard for new regimes/avg. hazard</td>
<td>3.04</td>
<td>2.04</td>
</tr>
<tr>
<td></td>
<td>(0.86)</td>
<td></td>
</tr>
<tr>
<td>Reform-hazard for new regimes/avg. hazard</td>
<td>6.90</td>
<td>8.95</td>
</tr>
<tr>
<td></td>
<td>(2.72)</td>
<td></td>
</tr>
<tr>
<td>Total transition hazard by $\lambda$: peak/autocracy</td>
<td>4.29</td>
<td>3.21</td>
</tr>
<tr>
<td></td>
<td>(1.92)</td>
<td></td>
</tr>
<tr>
<td>Total transition hazard by $\lambda$: democracy/autocracy</td>
<td>0.18</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>(0.16)</td>
<td></td>
</tr>
<tr>
<td>Median revolt</td>
<td>0.20</td>
<td>0.20</td>
</tr>
<tr>
<td></td>
<td>(0.02)</td>
<td></td>
</tr>
<tr>
<td>Median reform</td>
<td>0.80</td>
<td>0.80</td>
</tr>
<tr>
<td></td>
<td>(0.02)</td>
<td></td>
</tr>
<tr>
<td>Unconditional mass on $\lambda \leq 0.25$</td>
<td>0.42</td>
<td>0.47</td>
</tr>
<tr>
<td></td>
<td>(0.03)</td>
<td></td>
</tr>
<tr>
<td>Unconditional mass on $\lambda \geq 0.75$</td>
<td>0.42</td>
<td>0.47</td>
</tr>
<tr>
<td></td>
<td>(0.04)</td>
<td></td>
</tr>
</tbody>
</table>

Notes.—Bootstrap standard errors for the data, clustered at the country-level, are in parenthesis. All model moments are computed at the stationary distribution. The empirical moments are based on the data presented in Section 2.

co-occurrence of revolts and reforms, summarized by the ratio of revolts to reforms; (ii) the negative relation between transition hazards and regime maturity, summarized by the revolt and reform hazard for new regimes relative to the respective average hazards; (iii) the inverse J-shape of transition hazards in political inclusiveness, summarized by the hazard ratio at the peak of the inverse J-curve and at the most inclusive system ($\lambda = \lambda_{N_\lambda}$), both normalized relative to the least inclusive system ($\lambda = \lambda_{1}$); (iv) the polarization of new regimes, summarized by the median revolt and reform; and (v) the concentration of mass towards the extremes of the polity-distribution, $P(\lambda)$, summarized by $P(\lambda \leq 0.25)$ and $P(\lambda \geq 0.75)$.

Overall, the model fits the targeted moments quite well, with most model moments being within one standard deviation of their empirical counterpart. The exceptions are the distribution over $\lambda$, where the model over-predicts the concentration towards the extremes by 1.5 standard deviations, and the revolt hazard for new regimes, which the model under-predicts relative to the corresponding average rate. Despite some discrepancies, the estimated model is clearly able to replicate the documented regularities.
Untargeted moments For further evaluation of the model fit, we next study how well the model matches the precise shape of the transition hazards, conditional outcome distributions, and empirical distribution over $\lambda$ depicted in Figures 1–4. Beyond targeting the statistics in Table 2, none of these shapes are targeted in our calibration.

Figure 7 shows the corresponding relations for the estimated model. For convenience, the graphs also include the empirical relations from Section 2. Overall the model fits the data very well. We do not fully capture the shape of the relation between revolt hazard and regime maturity and we slightly underpredict the reform hazard for very mature regimes, but we capture the average rates at which these hazards decline in maturity—steeply for reforms and relatively slowly for revolts. Similarly, the model captures the inverse J-shape of transition hazards in inclusiveness, although it slightly underpredicts the hazard for the most inclusive regimes. Finally, the fit of the conditional outcome distributions and empirical distribution over $\lambda$ is almost perfect.

5 Understanding the Key Features of the Model

In this section, we provide intuition for how the different features of the model contribute to explaining the empirical facts.

Co-occurrence of revolts and reforms In the estimated model, revolts are almost three times as likely as reforms. Why are there so many coercive transitions if regimes could preempt any revolt by extending the franchise?

There are two reasons. First, reforms are costly so that regimes are willing to tolerate some risk of failure in order to hold on to power. If sharing power would bear no cost ($\alpha_u \to 0$), then clearly any regime would immediately transform to a perfectly inclusive democracy and there were no incentives to ever revolt. Second, as detailed in Proposition 2, asymmetric information reduces the effectiveness of reforms, which further tilts the regime towards holding on to power instead of reforming. If instead the realization of $\theta_t$ would be observed by outsiders, reforms have no signaling value and simply solve

$$x^{\text{sym}}(\lambda, \theta) = \arg\max_{x \in [\lambda, 1]} \hat{V}^I(\theta, \theta, x).$$

Generally, $x^{\text{sym}}$ lies strictly above the equilibrium schedule characterized in Proposition 2. I.e., not only are small reforms precluded by asymmetric information, but more generally they are biased downwards. As such, asymmetric information reduces the likelihood of reforms
Figure 7: Comparison between model (solid red lines) and data (crossed blue lines). None of the depicted relations are directly targeted in the calibration.
Table 3: Frequency of Revolts for Alternative Parameters and Without Asymmetric Information

<table>
<thead>
<tr>
<th>Cost of sharing power ($\alpha_u$)</th>
<th>Revolt–reform ratio</th>
<th>Autocracy–democracy ratio</th>
<th>Revolt–reform ratio</th>
<th>Autocracy–democracy ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.15</td>
<td>0.20</td>
<td>0.03</td>
<td>0.01</td>
<td>0.03</td>
</tr>
<tr>
<td>0.30</td>
<td>0.95</td>
<td>0.30</td>
<td>0.18</td>
<td>0.20</td>
</tr>
<tr>
<td>0.45</td>
<td>1.86</td>
<td>0.39</td>
<td>1.07</td>
<td>0.52</td>
</tr>
<tr>
<td>0.57</td>
<td>2.82</td>
<td>0.99</td>
<td>1.48</td>
<td>0.46</td>
</tr>
</tbody>
</table>

Notes.—The model is solved for different values of $\alpha_u$. All other parameters are fixed at their estimated values. The autocracy–democracy ratio defines the mass of regimes with $\lambda \leq .25$ relative to the mass of regimes with $\lambda \geq .75$ at the stationary distribution.

and tends to increase the likelihood of revolts (see Figure E.5 in the online appendix for an illustration).

To gauge the quantitative importance of each of these two factors, we re-solve the model for different values of $\alpha_u$ and for the case with symmetric information. All other parameters remain fixed at their estimated values. Table 3 reports the resulting revolt–reform ratios and the mass on “autocracies” (with $\lambda \leq .25$) relative to “democracies” (with $\lambda \geq .75$) at the stationary distribution. For the baseline calibration ($\alpha_u = .57$), both of the aforementioned factors contribute roughly equally to explaining the data: If information were symmetric, then the revolt–reform ratio drops below 1.5 (compared to 2.85 in the data), and $P(\lambda \geq .75)$ exceeds $P(\lambda \leq .25)$ by a factor of about two (compared to equal shares in the data).

**Transition hazards and maturity** Consider next the declining shape of transition hazards in regime maturity. The driving force behind this is a perceived “stabilization”, reflected in a decline in outsiders’ prior mean, $\mu_t$, as a regime becomes more mature. Specifically, from equation (11), it follows that for any $S_t$,

$$
\mu_{t+1} | (\text{reform}_t) \geq \mu_{t+1} | (\text{revolt}_t) > \mu_{t+1} | (\text{no transition}_t).
$$

(16)

After reforms (and revolts against reforming regimes), outsiders fully learn $\theta_t$, which conditionally on a reform is larger than $\bar{\theta}_t$. Similarly, Bayesian updating implies that $\theta_t$ is likely to be high when a revolt is observed in the absence of reforms. In contrast, when neither a reform nor a revolt are observed, Bayesian updating implies that $\theta_t$ is likely to be low. As a

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$^{21}$To see this, recall that $M^2$ defines the second raw moment, which is bounded by $(M^1)^2 < M^2 \leq M^1$ (the lower bound is strict as $\text{Var}_{\theta} [\theta_t] = M^2 - (M^1)^2 > 0$ for $x_t = \lambda_t$). Evaluating (11) at the upper and lower bound for $M^2$, respectively, and combining with (13) yields the two inequalities stated in (16).
regime ages, it is therefore perceived to be less and less vulnerable. Accordingly, joining a revolt becomes less and less attractive, reducing both the number of outsiders supporting a revolt and the incentives of insiders to reform. Moreover, if $\theta_t$ is unobserved to the statistician (as it is both in our computations and in the data), the belief effect is further strengthened by statistical selection, which, similarly to outsiders’ beliefs, places more probability mass on stable realizations of $\theta_t$ for older regimes.

Observe that (16) holds under any $F_t$ and does not hinge on the shape of $G$ (or on our Beta-approximation to (10)). To strengthen this point, consider the limit where $\Pr(\theta_t = \theta_{t-1}) \to 1$ ($\theta$ is fully persistent) and $F_t$ is computed exactly (without approximation).

Proposition 5. Let $G$ such that $\Pr(\theta_t = \theta_{t-1}) \to 1$. Then the revolt and reform hazards are decreasing in the maturity of a regime. Specifically, for any $S_0$, if $x_s = \lambda_0$ and $\eta_s = 0$ for all $s < t$, then

$$\Pr_t(\eta_t = 1) < \Pr_{t-1}(\eta_{t-1} = 1) \quad \text{and} \quad \Pr_t(x_t > \lambda_t) = 0.$$ 

Proposition 5 proves for perfectly persistent $\theta$ that the revolt and reform hazards are declining in regime maturity (regardless of whether or not $\theta_t$ is observed by the statistician). The decline in the reform hazard is especially stark, as it drops to zero for all but newly emerged regimes. While this extreme decline in the reform hazard is an artifact of $\Pr(\theta_t = \theta_{t-1}) \to 1$, it is reminiscent of the steep decline seen in the estimated model and the data.

Transition hazards and inclusiveness The inverse J-shape of transition hazards in $\lambda$ is the result of two opposing forces. On the one hand, as just explained, transition hazards are increasing in the prior mean $\mu_t$. On the other hand, transition hazards are declining in $\lambda_t$. The logic is similar to the one driving the dependence on $\mu_t$: As the regime becomes more inclusive, revolts are more likely to fail, which makes it even less attractive for remaining outsiders to support a revolt and further reduces incentives for insiders to reform.

These two forces are opposing, because $\mu_t$ is positively linked to $\lambda_t$ through statistical selection: As further detailed below, large regimes emerge from reforms, implying that they are perceived to be weak ($\bar{\mu}_{t-1} = \theta_{t-1} \geq \bar{\theta}_{t-1}$), whereas small regimes typically emerge from revolts against pooling regimes, implying that they are perceived to be relatively strong ($\bar{\mu}_{t-1} \leq \bar{\theta}_{t-1}$). Moreover, because $s$ is increasing in the perceived likelihood of success (Proposition 1), it is precisely revolts that ex-ante were considered as futile that give rise to the smallest regimes. Conversely, because $x$ is increasing in $\theta$ (Proposition 2), the largest regimes will be associated with being weakest upon their emergence.

\[\text{Revolts are more likely to succeed against pooling regimes, because reforms must be effective in reducing the threat of revolt to be observed in equilibrium.}\]
Figure 8: Intuition for inverse J-curve. Left panel: marginal transition hazard $E[haz|\mu, \lambda]$; solid black line traces contour of $(\mu, \lambda) = (E[\mu|\lambda], \lambda)$; red line depicts $E[haz|\lambda]$. Right panel: $E[\mu|\lambda]$. All expectations are computed at the stationary distribution.

Figure 8 illustrates these two forces. The right panel shows the statistical relation between $\mu_t$ and $\lambda_t$. The left panel plots the marginal transition probability with respect to $\mu_t$ and $\lambda_t$. The black line traces out the contour, $(\mu, \lambda) = (E[\mu|\lambda], \lambda)$, of the relation shown in the right panel, which closely approximates the exact J-curve $E[haz|\lambda]$ (depicted in red).

Relative to regimes at the center of the autocracy–democracy spectrum, full-scale democracies ($\lambda \rightarrow 1$) are stable due to a lack of opposition (dominating their perceived weakness). Extreme autocracies ($\lambda \rightarrow 0$), on the other hand, are similarly uncontested due to their perceived strength implying a low degree of coordination among outsiders.

Polarization of new regimes The logic behind the polarization of new regimes is straightforward. By Proposition 2, reforms are bounded below by $\xi(\bar{\theta}_t)$, since smaller reforms would be ineffective in reducing revolutionary pressure. Conversely, revolts cannot grow too large, since otherwise insiders would prefer to preempt them if they are vulnerable. In turn, outsiders

$^{23}$E[haz(E[μ|λ], λ)] is only approximate for two reasons. First, since the transition hazard is nonlinear in $\mu_t$, there is an approximation error associated with evaluating the hazard at the average $\mu$ for each $\lambda$ as depicted in the right panel (as opposed to computing the average hazard over the conditional distribution $\mu|\lambda$). Second, for our illustration, we have abstracted from the impact of $\sigma^2$ on the transition hazard, by marginalizing the hazard with respect to $\mu$ and $\lambda$, yielding another approximation error due to nonlinearity in $\sigma$. Comparing the approximation with the exact J-curve (in red), it can be seen that the difference is small, so that the main force behind the J-curve is indeed the statistical link between $\mu$ and $\lambda$ shown in the right panel.

$^{24}$Note that the result is not a mechanical consequence of reforms being bounded below by $\lambda_t$, which does not rule out that reforming autocracies become marginally larger autocracies. As evident from Figure 9 below, the lower bound is far from binding for autocracies, which conduct median reforms much larger than $\lambda_t$. 

26
can infer the regime to be strong if it does not preempt a large revolt, making it unattractive to join such a revolt in the first place. These considerations imply state-dependent bounds \( \bar{\lambda}^{\text{ref}}(\lambda_t, F_t) \) and \( \bar{\lambda}^{\text{rev}}(\lambda_t, F_t) \) such that for all \( \theta_t \in [0, 1] \),

\[
s_t \leq \bar{\lambda}^{\text{rev}}(\lambda_t, F_t) \quad \text{and} \quad x_t \geq \bar{\lambda}^{\text{ref}}(\lambda_t, F_t) \quad \text{for} \quad x_t \neq \lambda_t.
\]

While it is difficult to characterize these bounds fully analytically, it is possible to derive somewhat more conservative bounds, as stated in the following proposition.

**Proposition 6.** \( \bar{\lambda}^{\text{ref}}_t > 1 - (1 - \lambda_t)M^1_t(\tilde{\theta}_t)/\bar{\theta}_t \) and \( \bar{\lambda}^{\text{rev}}_t < (1 - \lambda_t)M^1_t(\tilde{\theta}_t) \).

For instance, if outsiders have a uniform prior \( (F_t(\theta) = \theta) \), then \( M^1_t(\tilde{\theta}_t) = \tilde{\theta}_t/2 \), implying \( \bar{\lambda}^{\text{ref}}_t > 1 - (1 - \lambda_t)/2 \) and \( \bar{\lambda}^{\text{rev}}_t < (1 - \lambda_t)/2 \). For a more general illustration, consider Figure 9.

Here we plot the median revolt and reform, computed conditionally on \( \lambda_t \), along with the 10th and 90th percentiles. The figure reveals that the polarization is strongest for transitions originating in regimes towards the extremes of the autocracy–democracy spectrum. The underlying logic is the flipside of the inverse J-curve: as extremely autocratic and democratic regimes face small equilibrium threats, only few outsiders revolt, and consequentially only regimes with large realizations of \( \theta_t \) reform. This implies low levels of \( s_t \) and large values of \( x_t = \xi(\theta_t) \).

**Stationary distribution** Finally, the bi-modal shape of the stationary distribution over polities is a simple corollary to the polarization of new regimes, depicted in panels (e) and (f) of Figure 7, and the inverse J-shape of the transition hazard in \( \lambda \), as shown in panel (c).
6 Model Implications for Democratization

In this section, we study the implications of the model for the formation and survival of democracies.

Outsiders’ sentiments and critical junctures In the model, the belief or “sentiment” of outsiders is instrumental for creating a window of opportunity, in which democratization is possible. Figure 10 illustrates the role of beliefs by plotting the predicted transition hazards as a function of $\mu_t$ (for fixed values of $\lambda$ and $\sigma$).\(^\text{25}\) If outsiders perceive the regime as sufficiently strong ($\mu_t$ is small), revolts constitute little threat and insiders abstain from reforms, independently from the current realization of $\theta_t$ (i.e., $\bar{\theta}(\lambda_t, F_t) = 1$). If, by contrast, outsiders perceive the regime as vulnerable, insiders anticipate them to coordinate on potentially large revolts and are inclined to implement democratic reforms to preempt them. Because reforms are effective in reducing revolutionary pressure, the revolt hazard is hump-shaped in $\mu_t$, even though the total transition hazard is increasing.

Interestingly, there is a region of intermediate values of $\mu_t$, in which both transition hazards are high. This is because insiders generally do not find it optimal to fully preempt revolts (see the discussion in the previous section). Periods with intermediate values of $\mu_t$ thus constitute “critical junctures”, during which small and random variations in current conditions determine whether a regime ultimately implements democratic reforms, is replaced by an autocracy, or

\(^{25}\)Here, $\lambda$ and $\sigma$ are fixed at .1 and .0475, respectively, but the relationship is largely insensitive in their precise values as long as $\lambda$ is not too large. For large values of $\lambda$, all three hazards are significantly reduced in their magnitude, while maintaining the same qualitative shape.
remains unchanged (see Acemoglu et al., 2008, 2009 for empirical evidence in support of such critical junctures). At the same time, because democracies and autocracies both stabilize once they mature, any system that eventually emerges at the end of a critical juncture is likely to persist for a long time.

**Illustration** Figure 11 shows the dynamic responses to a counterfactual change in outsiders’ beliefs, illustrating the arrival of a critical juncture and subsequent political stabilization. The time series is initialized at a “fully matured” autocracy, with $\lambda_0 = 0.1$ and beliefs given by their corresponding steady state values in the absence of any transition. As explained by the low value of $\mu_0$, the initial reform and revolt hazards are close to zero. The time path shows the response to a counterfactual change in outsiders’ beliefs at $t = 2$, resetting $F_2$ to a uniform prior.

As seen in the bottom three panels, the belief shock at $t = 2$ leads to an immediate rise in the reform hazard to roughly 20 percent and the revolt hazard to roughly 15 percent. Absent any transition, $\mu_t$ drops in the sequel, causing a sharp decline in the reform hazard and a moderate decline in the revolt hazard seen at $t = 3$ and $t = 4$. If the regime is overthrown, as we assume it is at the end of $t = 4$, we see another increase in $\mu_t$ and the transition hazards. Observe that this serial correlation of transition hazards implies that critical junctures often consist of multiple transition events.

In our illustration, we consider two alternative time paths. The solid red path shows how the autocracy stabilizes in the absence of further transitions, eventually leading to a reform hazard of zero and a revolt hazard that converges to less than 1 percent after roughly 100 periods. The dashed blue path shows how the time path diverges if instead insiders implement a democratic reform at $t = 6$, which occurs at a rate of 1.5 percent. Here, the inclusion of a large fraction of the population into the regime leads to an immediate drop in the revolt hazard to 2.7 percent, despite the strong increase in $\mu_t$. Absent further transitions, the reform hazard subsequently drops to zero and the revolt hazard eventually drops close to zero, albeit at a much smaller rate than before.

---

26Observe how marginal variations in $\lambda_t$ and $F_t$ can have large and persistent effects on $\lambda_{t+1}$ due to the discontinuity of $\hat{\theta}(\lambda_t, F_t)$ around $\theta_t$. Conditionally on $\lambda_t$ and $F_t$, outcomes are determined by the random realizations of $\theta_t$ and $\eta_t$.

27In the model, large belief changes are induced by (small-probability) transition events. While this means that the arrival of critical junctures is inextricably tied to regime changes, it is primarily the beliefs that are important for the subsequent dynamics. The experiment conducted here is designed to illustrate the pure impact of beliefs on transition probabilities by inducing the change in outsiders’ sentiments exogenously. While absent in the estimated model, it would be straightforward to incorporate noisy signals into our framework that would rationalize such belief shifts, capturing, for instance, sentiment shifts triggered by the deaths of political leaders or by events in neighboring countries as in Buera, Monge-Naranjo and Primiceri (2011).

28The rate of stabilization is low due to the large value estimated for $\rho$, which governs the “usefulness” of
Figure 11: Critical junctures and political stabilization. Solid red lines show the dynamic response to a counterfactual change in outsiders’ beliefs at $t = 2$ and a subsequent revolt at $t = 4$. Dashed blue lines show an alternative time path with an additional reform at $t = 6$. See the main text for further details.
Figure 12: Cumulative reversal rate of young democracies.

**Likelihood of successful democratization** From the illustration in Figure 11 it is evident that newly emerging democracies face a non-trivial probability of a regime reversal. This is because outsiders excluded from the franchise extension learn the regime’s vulnerability, leading to small but highly coordinated coup d’êts. To study the relevance of reversals more broadly, we have simulated a time series of 10 Million observations from the estimated model. Using this time path, we compute the reversal rate of young democracies (all new regimes with $\lambda \geq .75$) as a function of their maturity and the inclusiveness of the democracy at the time of its formation. The results are presented in Figure 12. Critical for the success of democratization is that the establishing reforms are comprehensive. Whereas the probability that a democracy with an initial polity of $\lambda \leq .85$ is overthrown in its first 25 periods is over 80 percent, the same probability drops to roughly 30 percent for democracies with an initial polity between .85 and .95, and drops to 12 percent for democracies that are initially larger than .95.

**Are democracies absorbing?** A related question is whether democracies are always bound to fail (albeit with a small probability), or if there is the possibility of an absorbing regime. In the model, transition hazards are strictly positive for any regime with $\lambda < 1$. Only a perfectly inclusive democracy with $\lambda = 1$ is absorbing. In the estimated version of the model, past information for forming beliefs regarding $\theta_t$. As $\theta_t$ is fully revealed through reforms, a high value of $\rho$ implies that new information has little effect on outsiders’ beliefs in the aftermath of a reform. Only over time, as the underlying state of $\theta_t$ changes (unobserved by outsiders) according to its law of motion, the precision of outsiders’ beliefs eventually falls and beliefs are adjusted at a higher rate. Here we do not count consecutive reforms as regime failures, so that the inclusiveness may change over the life time of a democracy.

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The image contains a graph with a legend indicating different ranges of maturity and inclusiveness for young democracies, and a cumulative reversal rate curve for each range. The x-axis represents maturity, and the y-axis represents the cumulative reversal rate.
this is ruled out by our discrete approximation to λ, as \( \lambda_{N} = .9875 \) (see Footnote 18 for details). But would an absorbing democracy eventually arise if we solved the model in a continuous state space? The answer depends on the value of \( \xi(1) \), which determines the largest democracy that is formed along the equilibrium path. Given the estimated value for \( \alpha \), we have \( \xi(1) = .978 \), so that fully inclusive democracies indeed do not emerge in equilibrium, even if we solve the model on a continuous polity space.

More generally, under which circumstances does an absorbing democracy emerge in equilibrium? From the boundary condition for \( \xi \), stated in Proposition 2, \( \xi(1) = 1 \) if \( \lim_{x \to 1} \hat{V}_3(1,1,x) \geq 0 \). Intuitively, this requires \( h(s(\cdot,x)) \) to be sufficiently steep around \( x = 1 \) to compensate for the cost of reforms, \( u'(1) \). With the parametrization for \( u \) and \( h \) used in the calibration, the condition reduces to a simple threshold in the elasticity of \( p \) with respect to \( s \).

**Proposition 7.** Let \( u(x) = 1+\alpha u(1-x) \) and \( h(s) = s^{\alpha h} \). Then, \( \xi(1) = 1 \) so that an absorbing democracy with \( \lambda \to 1 \) emerges along the equilibrium path (a.s.) if and only if \( \alpha h \leq .5 \).

If the success rate of revolts is relatively \textit{inelastic} in the number of supporters (\( \alpha h \leq .5 \)), outsiders’ coordination will not adjust strongly in response to reforms. To effectively reduce revolutionary pressure, insiders therefore mainly rely on the extensive margin of reforms, leading to (almost) absorbing democracies along the equilibrium path.\(^{30}\) By contrast, if \( \alpha h > .5 \), small groups of outsiders have a comparably low intensity of coordination and excluding them does not pose severe threats. In this case, democracies are always bounded away from \( \lambda = 1 \), so that reversals are observed with strictly positive probability against any regime.

7 Discussion

This section reviews alternative mechanisms for the empirical regularities documented in Section 2 that have been suggested by the literature. Existing works generally differ from the present paper in that they are not quantitative and make joint predictions for at most two of the five facts.

\(^{30}\)For a simple illustration, suppose there were no intensive margin of coordination; i.e., \( s_t = (1 - x_t)^{\tilde{\gamma}} \) for a constant \( \tilde{\gamma} \). Then \( \lim_{x \to 1} \hat{V}_3(1,1,x) = -\alpha u + \tilde{\gamma} \alpha h \lim_{x \to 1} s(1,x)^{\alpha h - 1} \), where the first term reflects the cost of reforms and the second term the reduction in the revolt threat. Clearly, as \( x \to 1 \) and \( s \to 0 \), the second term goes to \( \infty \). Hence, absent any intensive margin, regimes with \( \theta = 1 \) always prefer to establish a fully inclusive regime. By contrast, if there is a (sufficiently elastic) intensive margin, then as \( x \) increases, outsiders internalize the impact on \( p \) and coordinate less intensively. As a result, insiders face lower threats for large (but not fully inclusive) regimes, reducing the marginal benefit, \( -\partial h(s(\cdot,x))/\partial x \), of implementing fully inclusive reforms.
Co-occurrence of revolts and reforms  The present model already features two forces favoring the co-existence between revolts and (preemptive) reforms, both of which are also present in the existing literature. Specifically, asymmetric information has been used to rationalize revolts despite preemptive reforms in, e.g., Acemoglu and Robinson (2000a), Ellis and Fender (2011) and Boix (2003). Second, “gambling for survival”, which emerges when the benefits from holding on to power are sufficiently large relative to the likelihood that a revolt succeeds, has been previously present in Besley and Persson (2018). Finally, a third force, not present in our model, is limited commitment, which limits the compensation that can be credibly offered to outsiders so that conflict may arise whenever the constraint becomes binding (Acemoglu and Robinson, 2001; Acemoglu, Ticchi and Vindigni, 2010; Chassang and Padró i Miquel, 2009).

Transition hazards declining in maturity  In our model, transition hazards decline in regime maturity due to a reduced coordination among outsiders caused by learning. The literature has identified three alternative explanations, which in reduced form can be mapped into our framework as exogenous variations in $\theta$, $\gamma$ and $u$.

Specifically, a first strand of the literature has argued that young regimes are intrinsically more vulnerable compared to more mature ones (amounting to a drop in $\theta$ over time), because emerging democracies first need to establish institutions to disempower military leaders (Acemoglu, Ticchi and Vindigni, 2010) whereas emerging autocracies first need to establish institutions to effectively distribute economic rents to supporters (Svolik, 2009). A second strand of the literature has argued that societies become increasingly supportive of the current regime as political values adjust to political realities (Ticchi, Verdier and Vindigni, 2013; Besley and Persson, 2018), which in our framework could be interpreted as a shift in the distribution over political adjustment $\{\gamma_{i,t}\}$. Finally, Przeworski and Limongi (1997) offer empirical evidence that economic growth in the aftermath of democratization leads to political stabilization (see, however, Acemoglu et al., 2009). In the context of our framework, one possible interpretation would be that democratization may create an institutional environment supporting growth (e.g., Acemoglu and Robinson, 2008; Acemoglu, Ticchi and Vindigni, 2011), which over time increases the flow rents under democracy $u(\lambda \to 1)$ relative to other

31 Here we focus our discussion on revolts relating to preemptive reforms, because it is precisely the possibility of preemptive reforms that makes the prevalence of revolts puzzling in the first place. We are unaware of any work relating revolts to other (non-preemptive) types of reform.

32 The mechanism is related to Gallego and Pitchik (2004), who previously pointed out that autocratic leaders with long tenure are likely to have low costs of averting coups. As noted in Section 5, a similar selection effect arises in the present framework if the econometrician does not observe $\theta$, reinforcing the decline in hazards through learning.
regime types, reducing the chance of regime reversals.\textsuperscript{33}

Note that with the exception of Besley and Persson (2018), these explanations are specific to either autocratic or democratic consolidations. Our belief-driven explanation, by contrast, applies to all regime types, explaining the equally universal decline in hazards present in the data (see Online Appendix A.2 for empirical hazard curves by regime type).

**Inverse J-shape of transition hazards**  The notion that regime stability is J-shaped in inclusiveness has been coined by Bremmer (2006). In his monograph, Bremmer explains the “J-curve” with the ability of elites to control the information flow across society, which immanently varies across different regime types. While information is highly restricted in autocratic societies, inhibiting the coordination of revolts, it is precisely the free flow of information that enables democratic institutions to peacefully resolve any looming conflict. By contrast, intermediate regimes lack the institutions to preempt conflict whereas they are also ill-equipped to contain the spread of subversive ideas.\textsuperscript{34} An alternative account is given by Bueno de Mesquita et al. (2003), who refer to the distribution of wealth among elites across regime types to explain the J-curve. Specifically, Bueno de Mesquita et al. argue that democratic elites are more wealthy than elites in other societies due to a more efficient provision of public goods. Autocratic elites, by contrast, are similarly (albeit less) wealthy due to an efficient distribution of rents. Core supporters of intermediate regimes, by contrast, are less wealthy, because they lack both efficiency in the provision of public goods and in the distribution of rents. Accordingly, intermediate regimes are less supported, which is interpreted as instability.

Both of these arguments essentially imply that a regime’s polity $\lambda$ and its internal weakness $\theta$ are inextricably linked, while in our model this correlation arises endogenously. Through the lens of our model, the wealth of autocratic elites and their tight grip on information flows that explain the stability of autocratic systems in Bueno de Mesquita et al. and Bremmer may hence be the manifestation—instead of the source—of their internal strength.

\textsuperscript{33}At the level of individual leaders, Ales, Maziero and Yared (2014) explain a decline in exit rates through (self-enforcing) contracts, where re-elected leaders are those who get rewarded for compliant behavior, increasing their flow utility and hence their propensity of future compliance.

\textsuperscript{34}Likewise, Gates et al. (2006) point out that it may not be the better access to information but the better access to societal resources that facilitate political change in intermediate regimes. They note that, compared to heavily autocratic systems, the expansion of political participation gives “the opposition a better base from which to demand further decentralization” (p. 895).
Polarization of new regimes  Although we are aware of no other paper that endogenously predicts polarization towards both ends of the autocracy–democracy spectrum, there are a few papers that also predict that reforms are far-reaching in equilibrium. Closely related to our approach, Acemoglu and Robinson (2000a) predict that reforms tend to be fully inclusive in the presence of asymmetric information. In addition, both Justman and Gradstein (1999) and Jack and Lagunoff (2006b) predict incremental expansions of the franchise towards full democracy, but leave the scope of each reform unspecified. In particular, Justman and Gradstein argue that technological progress lowers the costs of higher redistribution associated with becoming more inclusive relative to a (reduced-form) benefit, leading to successive extensions of the suffrage in parallel to the industrial revolution. Jack and Lagunoff provide a more abstract trade-off for monotone franchise extensions where reforms are a means to implement future policies that are preferred but cannot be credibly enacted by current leaders. As the identity of the leader shifts over time, this leads to gradually larger and larger franchises. We are not aware of other works that endogenize the outcome of revolts.

Bimodal distribution  To the best of our knowledge, this paper is first to make predictions about the stationary distribution over regime types. The only other papers that we are aware of that can account for the bimodal distribution seen in the data, albeit mechanically, are Acemoglu and Robinson (2001) and Ticchi, Verdier and Vindigni (2013), in which regimes oscillate randomly between autocracy and democracy.

8  Final Remarks

We have developed a quantitative theory of repeated political transitions based on the evolution of beliefs regarding the regime’s strength. The model is distinguished from the existing literature by its ability to generate various patterns of regime change in a unified framework, including (possibly gradual) democratization processes, regime reversals against both emerging and mature democracies, and power struggles amongst autocratic regimes. We demonstrated the quantitative potential of the framework to match key facts from the data. Our results suggest that a simple model based on the interplay between revolutionary pressure and preemptive reforms can generate a process of political transitions that looks remarkably close to the data. Crucial for the close fit is the addition of an intensive margin of revolts, which links revolutionary pressure to the beliefs of outsiders regarding the regime’s strength: Precisely this link reduces the effectiveness of reforms, explaining the prevalence of revolts (fact 1). Similarly, the stabilization of mature and autocratic regimes (facts 2 and 3)
are both a direct consequence of reduced coordination along the intensive margin. Finally, absent an intensive margin, revolts would also mechanically increase for small $\lambda_t$, leading to counterfactually large revolts that are at odds with fact 4.

References


